

Formal Languages, Automata and Codes

Oleg Gutik



Lecture 18

6.2 Two Important Normal Forms

There are many kinds of normal forms we can establish for context-free grammars. Some of these, because of their wide usefulness, have been studied extensively. We consider two of them briefly.

Chomsky Normal Form

One kind of normal form we can look for is one in which the number of symbols on the right of a production is strictly limited. In particular, we can ask that the string on the right of a production consist of no more than two symbols. One instance of this is the *Chomsky normal form*.

Definition 6.4

A context-free grammar is in *Chomsky normal form* if all productions are of the form

$$A \rightarrow BC$$

or

$$A \rightarrow a,$$

where A, B, C are in V , and a is in T .

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Example 6.7

The grammar

$$S \rightarrow AS|a,$$

$$A \rightarrow SA|b$$

is in Chomsky normal form. The grammar

$$S \rightarrow AS|AAS,$$

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is not; both productions $S \rightarrow AAS$ and $A \rightarrow aa$ violate the conditions of Definition 6.4.

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Theorem 6.6

Any context-free grammar $G = (V, T, S, P)$ with $\lambda \notin L(G)$ has an equivalent grammar $\hat{G} = (\hat{V}, \hat{T}, S, \hat{P})$ in Chomsky normal form.

Proof. Because of [Theorem 6.5](#), we can assume without loss of generality that G has no λ -productions and no unit-productions. The construction of \hat{G} will be done in two steps.

Step 1. Construct a grammar $G_1 = (V_1, T, S, P_1)$ from G by considering all productions in P in the form

$$A \rightarrow x_1 x_2 \cdots x_n, \quad (1)$$

where each x_i is a symbol either in V or in T . If $n = 1$ then x_1 must be a terminal since we have no unit-productions. In this case, put the production into P_1 . If $n \geq 2$ then introduce new variables B_a for each $a \in T$. For each production of P in the form (1) we put into P_1 the production

$$A \rightarrow C_1 C_2 \cdots C_n,$$

where

$$C_i = x_i \text{ if } x_i \text{ is in } V,$$

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For every B_a we also put into P_1 the production

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Any context-free grammar $G = (V, T, S, P)$ with $\lambda \notin L(G)$ has an equivalent grammar $\hat{G} = (\hat{V}, \hat{T}, S, \hat{P})$ in Chomsky normal form.

Proof. Because of [Theorem 6.5](#), we can assume without loss of generality that G has no λ -productions and no unit-productions. The construction of \hat{G} will be done in two steps.

Step 1. Construct a grammar $G_1 = (V_1, T, S, P_1)$ from G by considering all productions in P in the form

$$A \rightarrow x_1 x_2 \cdots x_n, \quad (1)$$

where each x_i is a symbol either in V or in T . If $n = 1$ then x_1 must be a terminal since we have no unit-productions. In this case, put the production into P_1 . If $n \geq 2$ the introduce new variables B_a for each $a \in T$. For each production of P in the form (1) we put into P_1 the production

$$A \rightarrow C_1 C_2 \cdots C_n,$$

where

$$C_i = x_i \text{ if } x_i \text{ is in } V,$$

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For every B_a we also put into P_1 the production

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This part of the algorithm removes all terminals from productions whose right side has length greater than one, replacing them with newly introduced variables. At the end of this step we have a grammar G_1 all of whose productions have the form

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Example 6.8

Convert the grammar with productions

$$S \rightarrow ABa,$$

$$A \rightarrow aab,$$

$$B \rightarrow Ac$$

to Chomsky normal form.

As required by the construction of Theorem 6.6, the grammar does not have any λ -productions or any unit-productions.

In Step 1, we introduce new variables B_a, B_b, B_c and use the algorithm to get

$$S \rightarrow ABB_a,$$

$$A \rightarrow B_a B_a B_b,$$

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Example 6.8 (continuation)

In the second step, we introduce additional variables to get the first two productions into normal form and we get the final result

$$S \rightarrow AD_1,$$

$$D_1 \rightarrow BB_\alpha,$$

$$A \rightarrow B_\alpha D_2,$$

$$D_2 \rightarrow B_\alpha B_\beta,$$

$$B \rightarrow AB_\gamma,$$

$$B_\alpha \rightarrow a,$$

$$B_\beta \rightarrow b,$$

$$B_\gamma \rightarrow c.$$

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Another useful grammatical form is *Greibach normal form*. Here we put restrictions not on the length of the right sides of a production, but on the positions in which terminals and variables can appear. Arguments justifying Greibach normal form are a little complicated and not very transparent. Similarly, constructing a grammar in Greibach normal form equivalent to a given context-free grammar is tedious. We therefore deal with this matter very briefly. Nevertheless, Greibach normal form has many theoretical and practical consequences.

Definition 6.5

A context-free grammar is said to be in *Greibach normal form* if all productions have the form

$$A \rightarrow ax,$$

where $a \in T$ and $x \in V^*$.

If we compare this with [Definition 5.4](#), we see that the form $A \rightarrow ax$ is common to both Greibach normal form and s -grammars, but Greibach normal form does not carry the restriction that the pair (A, a) occur at most once. This additional freedom gives the Greibach normal form a generality not possessed by s -grammars.

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where $a \in T$ and $x \in V^*$.

If we compare this with [Definition 5.4](#), we see that the form $A \rightarrow ax$ is common to both Greibach normal form and s -grammars, but Greibach normal form does not carry the restriction that the pair (A, a) occur at most once. This additional freedom gives the Greibach normal form a generality not possessed by s -grammars.

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Example 6.9

The grammar

$$S \rightarrow AB,$$

$$A \rightarrow aA|bB|b,$$

$$B \rightarrow b$$

is not in Greibach normal form. However, using the substitution given by Theorem 6.1, we immediately get the equivalent grammar

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Here we can use a device similar to the one introduced in the construction of Chomsky normal form. We introduce new variables A and B that are essentially synonyms for a and b , respectively. Substituting for the terminals with their associated variables leads to the equivalent grammar

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